

Chapter 5

List all pairs of factors of each integer.

(5-1)

1. 42 2. 80 3. 91 4. 72 5. 52

6–10. Find the prime factorization of each integer in Exercises 1–5.

Give the GCF of each group of numbers.

(5-1)

11. 126, 168 12. 144, 84 13. 65, 52 14. 90, 330

Simplify. Assume that no denominator equals 0.

(5-2)

15. $\frac{12x^5}{4x}$ 16. $\frac{25m^4n}{-15mn^6}$ 17. $\frac{-7ab}{21ab^5}$ 18. $\frac{-8(uv)^7}{-10(uv)^5}$
19. $\frac{(w^4)^2}{(w^5)^4}$ 20. $\frac{(5k)^2}{5k^2}$ 21. $\frac{(-3y)^3}{(y^3)^2}$ 22. $\frac{(2c^5)(4c^3)}{(8c^2)^3}$

Divide.

(5-3)

23. $\frac{12e + 8}{4}$ 24. $\frac{6x - 9y + 12}{3}$ 25. $\frac{2x^3 + 6x^2 + x}{x}$
26. $\frac{18ab - 24a^2}{-6a}$ 27. $\frac{15m - 25m^2 - 5m^3}{5m}$ 28. $\frac{28h^5k^3 - 35hk^2}{7hk^2}$

Factor each polynomial as the product of its greatest monomial factor and another polynomial.

(5-3)

29. $15w^2 - 10w + 5$ 30. $9x^2 + 18x$ 31. $7u^3 + 14u^2$
32. $12a^3 - 6a^2 + 18a$ 33. $15c^2 + 3cd$ 34. $8m^2n - 24mn^2$

Write each product as a trinomial.

(5-4)

35. $(x + 5)(x + 3)$ 36. $(b - 2)(b - 4)$ 37. $(n - 3)(n + 7)$
38. $(e - 8)(e + 6)$ 39. $(3 + m)(2 + m)$ 40. $(3f + 2)(f + 5)$
41. $(4y - 3)(2y - 1)$ 42. $(8z + 7)(z - 2)$ 43. $(5n - 3)(4n - 2)$
44. $a(6a - 4)(5a - 3)$ 45. $h(3h + 7)(4h + 9)$ 46. $2x(9x - 1)(2x + 3)$

Write each product as a binomial.

(5-5)

47. $(k - 5)(k + 5)$ 48. $(3 - y)(3 + y)$ 49. $(4d - 8)(4d + 8)$
50. $(w^2 - 6)(w^2 + 6)$ 51. $(5m^2 + n)(5m^2 - n)$ 52. $(ab + c^2)(ab - c^2)$

Factor. You may use a calculator or the table of squares.

(5-5)

53. $16e^2 - 9$ 54. $36u^2 - 25$ 55. $81 - f^2$ 56. $144a^2 - 64b^2$
57. $49 - 100y^2$ 58. $v^4 - w^4$ 59. $s^6 - 4$ 60. $16x^8 - 625$

Express each square as a trinomial.

(5-6)

61. $(g + 7)^2$

62. $(k - 3)^2$

63. $(2x + 6)^2$

64. $(5y - 3)^2$

65. $(2m + 3n)^2$

66. $(7a - 5b)^2$

67. $(ef - 8)^2$

68. $(-4 + 9f)^2$

Factor.

(5-6)

69. $x^2 - 6x + 9$

70. $e^2 + 18e + 81$

71. $4 - 28h + 49h^2$

72. $64x^2 + 80xy + 25y^2$

73. $4m^2 - 36mn + 81n^2$

74. $16w^2 + 24wz + 9z^2$

Factor. Check by multiplying the factors. If the polynomial is not factorable, write *prime*.

(5-7, 5-8, 5-9)

75. $k^2 + 8k + 7$

76. $v^2 - 9v + 20$

77. $a^2 - 2a + 1$

78. $35 + 12u + u^2$

79. $n^2 - 16n + 48$

80. $w^2 + 18w + 80$

81. $x^2 + 13xy + 42y^2$

82. $m^2 - 10mn + 21n^2$

83. $e^2 - 15ef + 44f^2$

84. $c^2 + 3c - 18$

85. $x^2 - 2x - 35$

86. $k^2 + 8k - 32$

87. $h^2 - 7h - 18$

88. $b^2 + 7b - 30$

89. $y^2 - 4y - 45$

90. $a^2 - 2ab - 3b^2$

91. $u^2 + 3uv - 4v^2$

92. $m^2 - mn - 20n^2$

93. $2x^2 + 11x + 12$

94. $10e^2 - 12e + 3$

95. $10d^2 + d - 3$

96. $-10 - 26y - 12y^2$

97. $-7 - 39z - 18z^2$

98. $-10 + 24z - 8z^2$

99. $15x^2 + 13xy + 2y^2$

100. $8a^2 - 22ab + 12b^2$

101. $14m^2 - mn - 3n^2$

Factor. Check by multiplying.

(5-10)

102. $8(m - 3) - 5m(3 - m)$

103. $6a(a + 2) + 4(a + 2)$

104. $u(u - 2v) - (2v - u)$

105. $b(b - 2)(b + 1) - 3 - 3b$

106. $a^2 + 2a + ab + 2b$

107. $7cw + 3c - 7w^2 - 3w$

108. $n^3 + n^2 - 6n - 6$

109. $64 - 64m^2 + m^4 - m^6$

Factor completely. Check by multiplying.

(5-11)

110. $42x^3 + 68x^2 + 16x$

111. $60y^3 - 18y^2 - 6y$

112. $12x^5 - 20x^4 + 3x^3$

113. $16a^4 - 144a^2$

114. $4n^5 - 100n$

115. $28w^7 - 102w^5$

116. $36m^2 + 24mn + 4n^2$

117. $24cd - 12c^2 - 12d^2$

118. $-7x^3 + 14x^2y - 7xy^2$

Solve and check.

(5-12)

119. $(a + 13)(a + 8) = 0$

120. $(f - 16)(f - 27) = 0$

121. $(2x - 4)(3x - 5) = 0$

122. $(6h - 5)(6h + 5) = 0$

123. $7w(4w + 3) = 0$

124. $m(2m + 7)(3m - 4) = 0$

125. $a^2 + 7a + 6 = 0$

126. $q^2 - 21q = -20$

127. $d^2 = 14d - 45$

128. $y^2 - 7y - 18 = 0$

129. $c^2 - 36 = -5c$

130. $h^2 = -3h + 54$

131. $6 - 23z - 4z^2 = 0$

132. $3m^2 + 1 = 4m$

133. $2n^2 = 10 + n$

134. $e^2 - 49 = 0$

135. $36g^2 = 16$

136. $w^3 - 9w = 0$

137. The sum of a number and its square is 56. Find the number.
138. Find two consecutive negative odd integers whose product is 143.
139. The length of a rectangle is 5 cm less than twice the width. If the area of the rectangle is 88 cm^2 , find the dimensions of the rectangle.
140. Find two numbers that total 12 and whose squares total 74.

(5-13)

Chapter 6

Simplify. Give the restrictions on the variable.

(6-1)

1. $\frac{5m-15}{m-3}$
2. $\frac{2a+1}{6a+3}$
3. $\frac{7c-7d}{7c+7d}$
4. $\frac{6k-k^2}{36-k^2}$
5. $\frac{3uv}{u^2v-v^2u}$
6. $\frac{8w^3}{8w^2-12w}$
7. $\frac{x^2-64}{x^2-x-56}$
8. $\frac{(e-7)^2}{49-e^2}$
9. $\frac{15m+6n}{25m^2-4n^2}$
10. $\frac{a^2+ab}{a^2-ab}$
11. $\frac{(k-3)(7k-2)}{(2-7k)(k-3)}$
12. $\frac{3x^2+17xy+20y^2}{3x^2-xy-10y^2}$
13. $\frac{14-9t+t^2}{t^2-4}$
14. $\frac{u^2-v^2}{u^2+2uv+v^2}$
15. $\frac{(5w-x)^5}{(x-5w)^7}$
16. $\frac{(4s-6)^2(3s-2)}{(2-3s)(6-4s)}$

Multiply. Express each product in simplest form.

(6-2)

17. $\frac{5}{8} \cdot \frac{32}{15}$
18. $\frac{4}{3} \cdot \frac{3}{5} \cdot \frac{5}{7}$
19. $\left(\frac{-2}{5}\right)^2 \cdot \frac{15}{16}$
20. $\left(-\frac{3}{2}\right)^3 \cdot \frac{24}{9}$
21. $\frac{e}{f} \cdot \frac{f}{g} \cdot \frac{g}{h}$
22. $\frac{5}{w} \cdot \frac{w^2}{10}$
23. $\frac{8m}{3} \cdot \frac{9}{12m}$
24. $\frac{a^2}{3b} \cdot \frac{b^2}{4a}$
25. $\frac{14v}{12v^2} \cdot \frac{4uw^2}{7v^2}$
26. $\frac{a+5}{a} \cdot \frac{a^2}{a^2-25}$
27. $\frac{4x-xy}{8x^2y} \cdot \frac{2}{16-y^2}$
28. $\frac{m+n}{m-n} \cdot \frac{m^2-n^2}{3m+3n}$

Simplify. Use the rules of exponents for a power of a product and a power of a quotient.

(6-2)

29. $(5k^3)^2$
30. $\left(\frac{x}{7}\right)^2$
31. $\left(\frac{3x}{4}\right)^2$
32. $\left(\frac{2m}{3n^2}\right)^3$
33. $\left(-\frac{x^2}{5}\right)^3$
34. $\left(\frac{e}{f}\right)^3 \cdot \frac{e}{f}$
35. $\left(\frac{4c}{d}\right)^3 \cdot \frac{c^2}{8}$
36. $\left(\frac{7a}{b}\right)^2 \cdot \frac{3ab}{14}$